

EoS

The Equation of State used here is:

$$V = nV_0 e^{\frac{-p}{ap+bp^2+K_0} + (\alpha_0 + cp + dp^2)T} \left(1 + \frac{cp + dp^2}{\alpha_0}\right)^f gT^2 \quad (1)$$

where, a is a linear, b is a quadratic term for the pressure dependence of the bulk modulus, c is a linear and d is a quadratic term for the pressure dependence of the volume coefficient of thermal expansion and f and g are parameters describing the temperature dependence of the volume coefficient of thermal expansion. The theoretical explanations for Eq. (1) and the physics of the parameters are discussed in detail [1]. The equation has an analytical solution for the temperature

$$T = \frac{-(\alpha_0 + cp + dp^2) \pm \sqrt{(\alpha_0 + cp + dp^2)^2 + 4g \left(1 + \frac{cp + dp^2}{\alpha_0}\right)^f \left[\ln\left(\frac{V}{V_0}\right) + \frac{p}{ap + bp^2 + K_0}\right]}}{2g \left(1 + \frac{cp + dp^2}{\alpha_0}\right)^f} \quad (2)$$

The pressure is determined by repeated substitutions as:

$$p = \lim_{n \rightarrow \infty} f^n(p) \quad (3)$$

where

$$f^n(p) = (K_0 + ap_{n-1} + bp_{n-1}^2) \left[(\alpha_0 + cp_{n-1} + dp_{n-1}^2) T + \left(1 + \frac{cp_{n-1} + dp_{n-1}^2}{\alpha_0}\right)^f gT^2 - \ln\left(\frac{V}{V_0}\right) \right] \quad (4)$$

$$n \in \mathbb{N}^* \quad \text{and} \quad p_0 = 0$$

The convergence of Equation (4) depends on pressure. For the maximum pressure used in this study (up to 140 GPa) n = 15 is sufficient. The maximum convergence error $[\varepsilon]$ for the investigated data set is 0.05 GPa where

$$\varepsilon \geq |f^{15}(p) - f^{14}(p)|. \quad (5)$$